

# Understanding Subsumption of First- and Second-Order Mutants

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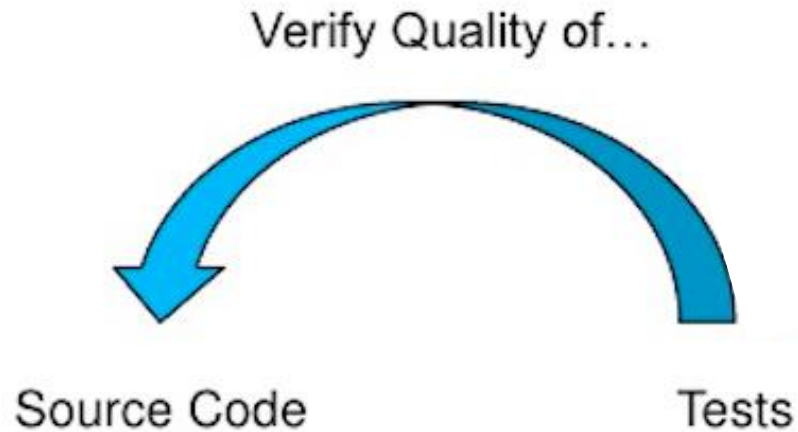
# Outline

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- ❑ Mutation testing
- ❑ Mutants subsumption
- ❑ Dynamic mutant subsumption graphs
- ❑ Study design
- ❑ Preliminary results
- ❑ Comparison with SS2OMs reduction
- ❑ Final remarks

# Introduction

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# Mutation Testing

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- Introducing **artificial syntactic changes (mutations)** into original source code
  - Intending to represent real common programming bugs
  - Changed programs are called **mutants**
- Running test cases on mutants
  - Result different from original: mutant **killed**
  - Otherwise: **alive**

# Example of a mutant

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Mutation place:

```
public class Taxes {  
  
    double simpleTax(double amount) {  
  
        return amount * 0.2;  
    }  
}
```

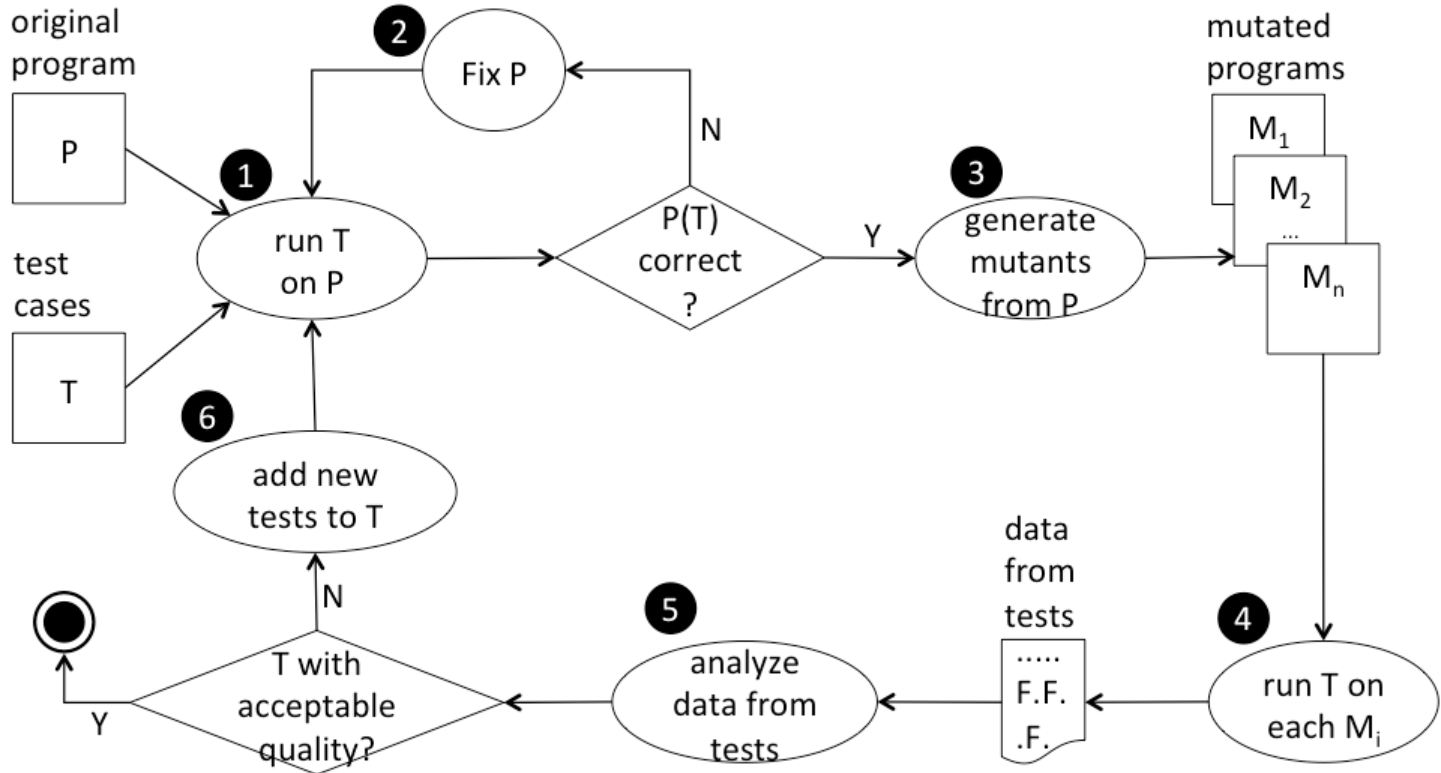
# Example of a mutant

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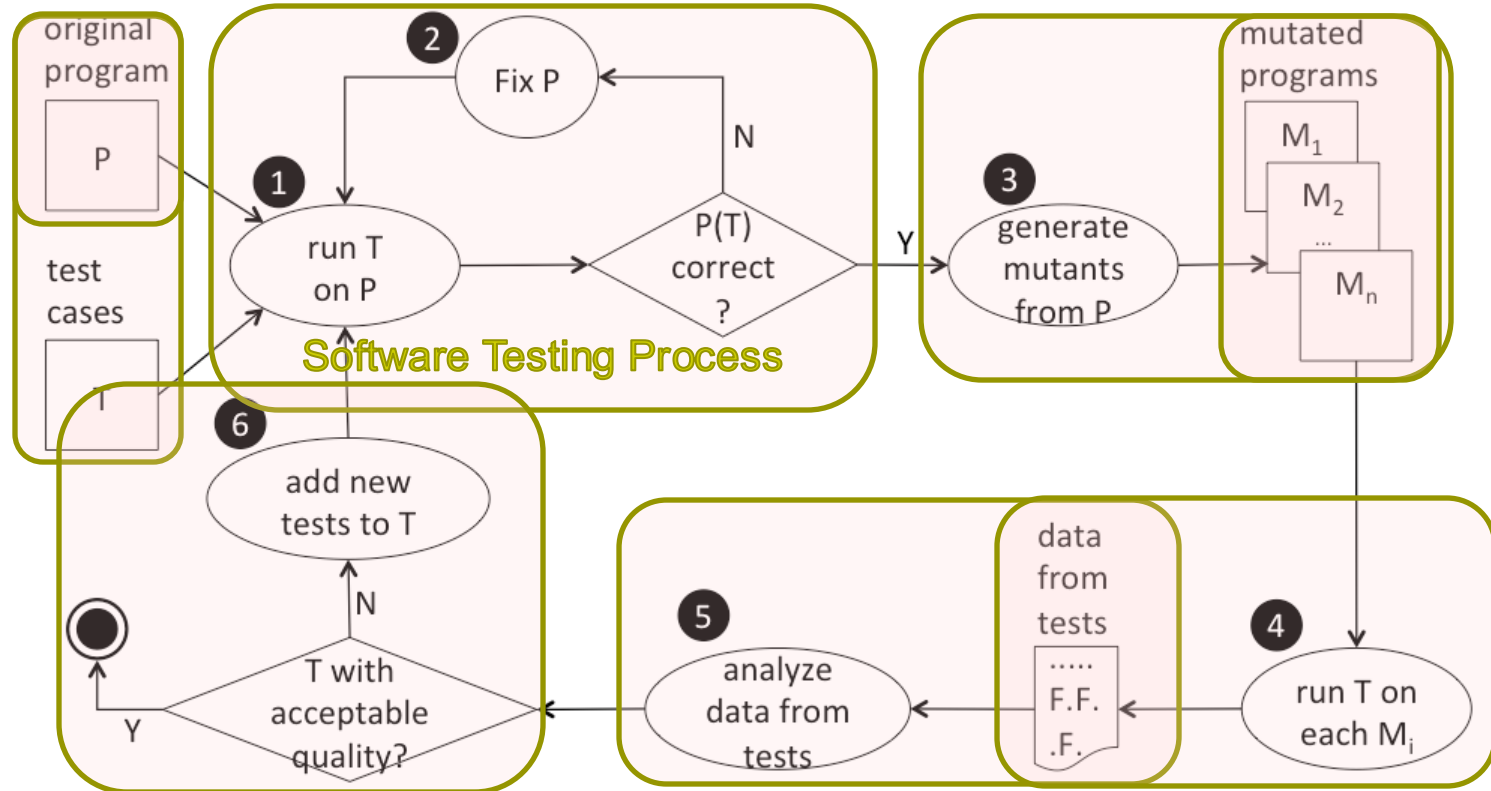
\* → +

```
public class Taxes {  
  
    double simpleTax(double amount) {  
  
        return amount + 0.2;  
    }  
}
```

# Mutation testing process



# Mutation testing process





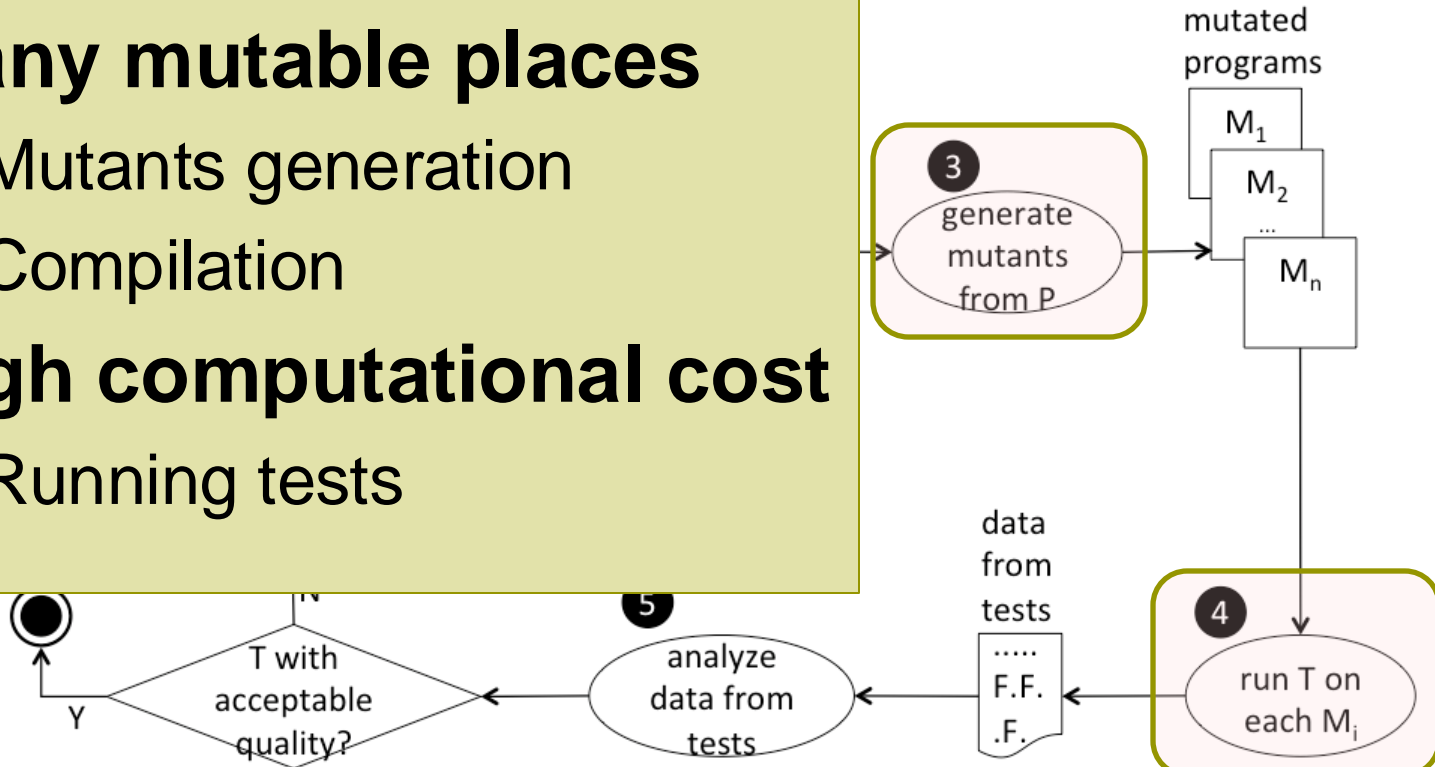
# Mutation testing drawbacks

## 3. Many mutable places

- Mutants generation
- Compilation

## 4. High computational cost

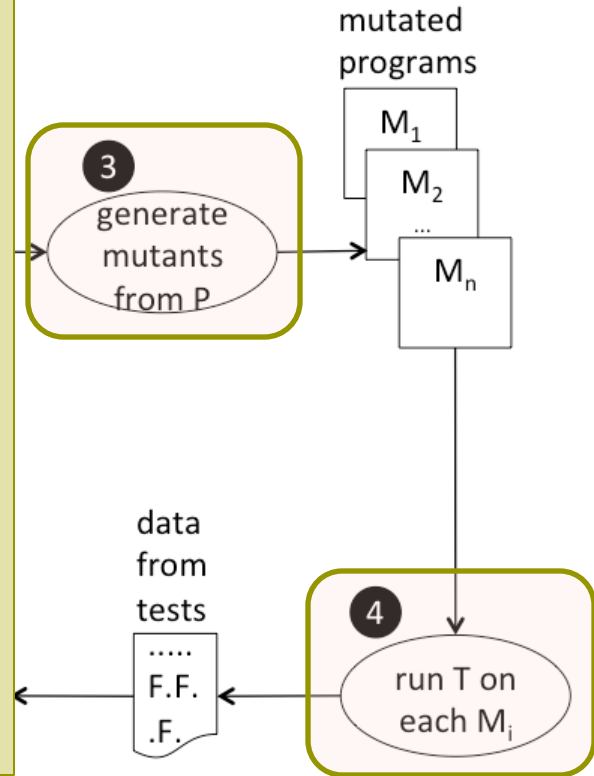
- Running tests



# Mutation testing drawbacks

## □ Cost reduction techniques

- Number of test cases
- Test case prioritization
- Number of mutants
  - **subsumption**





# Mutants subsumption

# Contextualization

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```
def greaterThan(a, b):  
    return a > b    # original  
    return a >= b   # mutant 1  
    return a <= b   # mutant 2
```

# Contextualization

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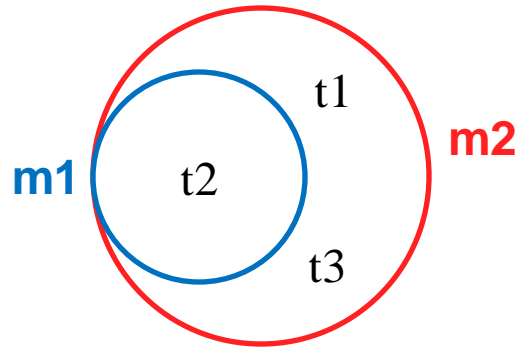
```
def greaterThan(a, b) :  
    return a > b # original  
    return a >= b # mutant 1  
    return a <= b # mutant 2
```

	Test	orig	m1	m2
t1	assertTrue(greaterThan(6, 5))	✓	✓	✗
t2	assertFalse(greaterThan(5, 5))	✓	✗	✗
t3	assertFalse(greaterThan(5, 6))	✓	✓	✗

# Contextualization

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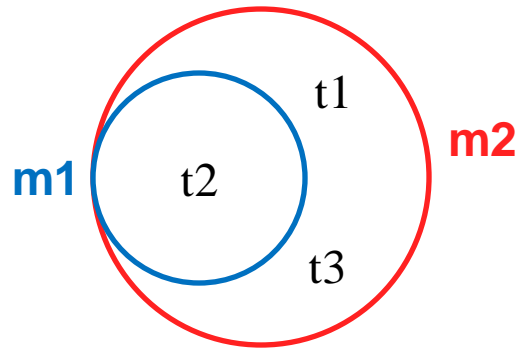
- Killing tests



# Contextualization

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- All test sets that kill **m1** also kill **m2**



# Definition

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- The notion of **subsumption** is used to compare **test criteria**:

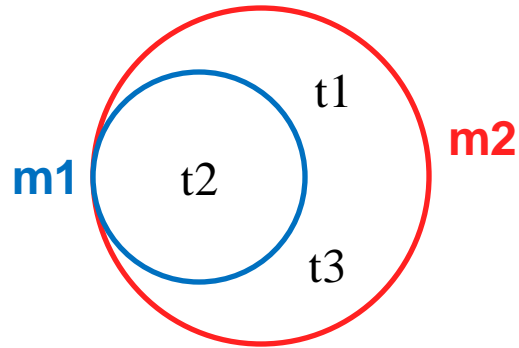
*"a criterion C1 **subsumes** C2 if every set of tests that satisfy C1 also satisfy C2"*



# Conclusion

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- **m1** subsumes **m2**



# Conclusion

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- If we know beforehand that
  - **m1** subsumes **m2**
- Therefore,
  - **m2** should not have been generated

Cost reduction: fewer mutants to run the test suite against



# Dynamic mutant subsumption graphs

# Example

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test	m1	m2	m3	m4	m5
t1	✗	✗		✗	✗
t2	✗		✗	✗	
t3				✗	
t4		✗		✗	✗

# Subsumption relationships

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test	m1	m2	m3	m4	m5
t1	✗	✗		✗	✗
t2	✗		✗	✗	
t3				✗	
t4		✗		✗	✗

m1 → m4

m2 → m4

m3 → m1

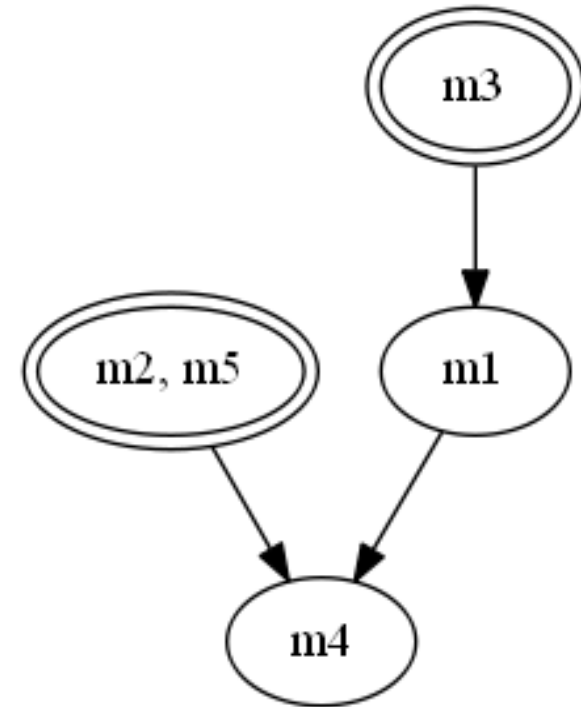
m3 → m4

m5 → m4

# Subsumption graph

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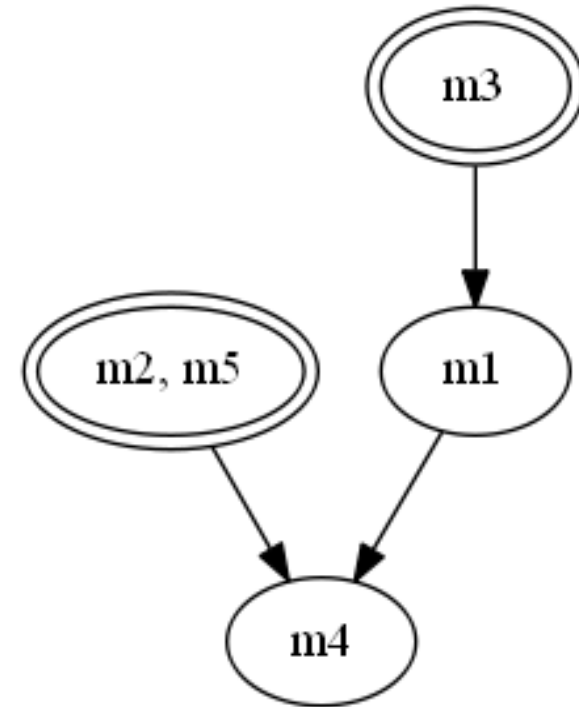
Test	m1	m2	m3	m4	m5
t1	✗	✗		✗	✗
t2	✗		✗	✗	
t3				✗	
t4		✗		✗	✗



# Conclusion

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- ❑ **Root nodes are kept**
  - 2 minimal
  - 3 mutants
- ❑ **Remaining nodes**
  - are disregarded
  - (redundants)





# Study design



# Dataset: 9 Java systems

System	Version	LOC	# Tests	JUnit	+16K mutants
Vending Machine	Exceptions	~100	35	4	<b>57</b>
Triangle	n/a	34	12	4	<b>138</b>
Monopoly	n/a	1,181	124	3	<b>866</b>
Commons CSV	1.8	~2k	325	4	<b>925</b>
Commons CLI	1.4	2,699	318	4	<b>1,082</b>
ECal	2003.10	3,626	224	3	<b>1,207</b>
Commons Validator	1.6	7,409	536	4	<b>3,197</b>
Gson	2.9.0	> 10k	1,089	3 and 4	<b>3,712</b>
Chess	n/a	4,924	930	3 and 4	<b>5,287</b>

# Study steps

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- Compute the killing tests for each mutant
- Generate the subsumption graph
- Retrieve the root (minimal) nodes



# Preliminary results

# Subsumption analysis

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System	mutants	minimal nodes	remaining mutants
Vending Machine	57	8	19
Triangle	138	12	59
Monopoly	866	48	127
Commons CSV	925	79	260
Commons CLI	1,082	101	238
ECal	1,213	98	281
Commons Validator	3,197	137	858
Gson	3,712	288	876
Chess	5,319	344	1,018
<b>Total</b>	<b>16,471</b>	<b>1,115</b>	<b>3,376</b>

# Highlight on Triangle

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## 12 minimal nodes:

{91}

{65, 67, 68, 70, 75, 77, 80, 52, 85, 56, 57, 58, 59, 63}

{35, 37, 38, 39, 108, 112, 114, 115, 116, 118, 119}

{129, 130, 131, 46, 122, 123, 124, 127}

{11}

{62}

{79}

{5}

{96, 132, 136, 121, 106, 111}

{69}

{97, 99, 100, 101, 103, 104, 23, 24, 25, 26, 27, 28, 93}

{0}

# Comparison with SS2OMs reduction

# Isolated reductions

System	FOMs	Via subsumption graph	Via SS2OMs
Vending Machine	57	66,67%	14.04%
Triangle	138	57,25%	36.23%
Monopoli	866	85,33%	24.13%
Commons CSV	925	71,89%	20.32%
Commons CLI	1,082	78,00%	31.05%
ECal	1,213	76,83%	22.54%
Commons Validator	3,197	73,01%	24.52%
Gson	3,712	76,40%	20.42%
Chess	5,319	80,86%	20.38%
<b>Overall</b>	<b>16,471</b>	<b>77.35%</b>	<b>22.37%</b>

# Isolated r

System		Ms
Vending Machine		
Triangle		
Monopoli		
Commons CSV		
Commons CLI		
ECal		
Commons Validator		
Gson		
Chess		
<b>Overall</b>	<b>16,471</b>	<b>77.35%</b>







# Final remarks

# Investigate

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- Can SS2OMs reduce even more the non-subsumed mutants?
- Is it correct keeping only one mutant from each minimal set?

# Reference

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B. Kurtz, P. Ammann, M. E. Delamaro, J. Offutt and L. Deng  
**Mutant Subsumption Graphs, 2014**  
*IEEE Seventh International Conference on Software Testing  
Verification and Validation Workshops (Mutation)*  
Cleveland, OH, USA, pp. 176-185  
doi: 10.1109/ICSTW.2014.20.



Questions?

